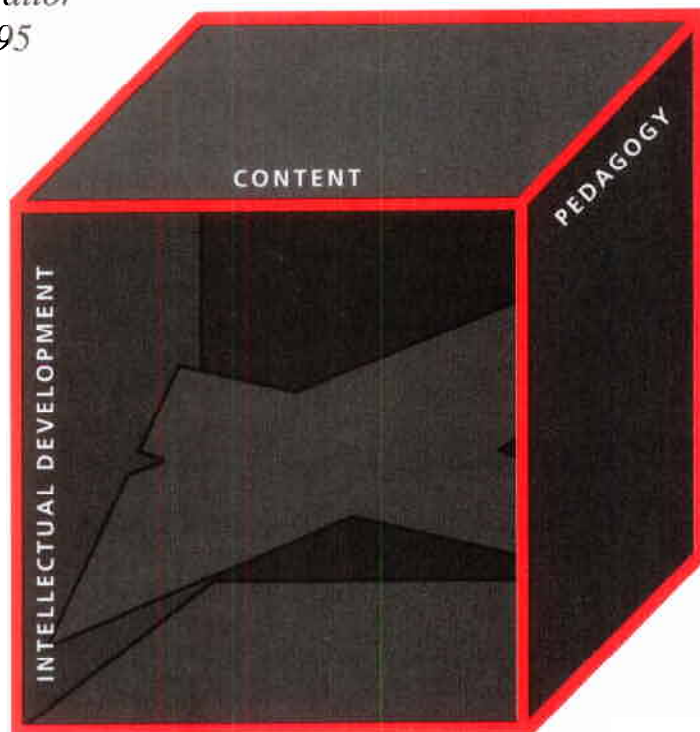


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# CROSSROADS IN MATHEMATICS

## Standards for Introductory College Mathematics before Calculus

*Prepared by the Writing Team and Task Force  
of the Standards for Introductory  
College Mathematics Project,  
Don Cohen, Editor  
September 1995*



American Mathematical Association  
of Two-Year Colleges



Funding for this project has been furnished by the National Science Foundation (DUE-9255850), the Exxon Education Foundation, Texas Instruments Incorporated, and the American Mathematical Association of Two-Year Colleges. The opinions expressed in this document do not necessarily reflect those of the National Science Foundation, the Exxon Education Foundation, or Texas Instruments Incorporated.

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*Crossroads in Mathematics: Standards for Introductory College Mathematics Before Calculus*/American Mathematical Association of Two-Year Colleges.

ISBN 0-9643890-0-2

Library of Congress Catalog Card Number: 95-77636

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